

$$e_1(t) = 100\sqrt{2} \sin 100t$$

$$e_2(t) = 100\sqrt{2} \sin 100t + \pi/2$$

$$R_1 = 2.5 \Omega \quad R_2 = 10 \Omega \quad R_3 = 10 \Omega$$

$$L_1 = 200 \text{ mH} \quad C_1 = 1 \text{ mF}$$

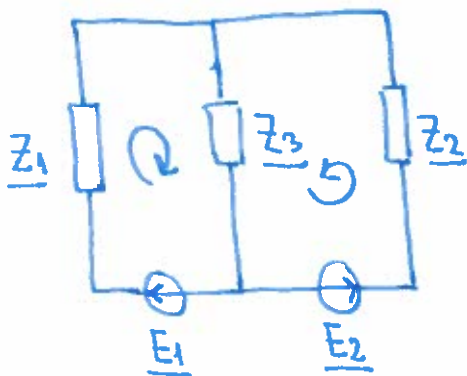
$$C_2 = 1 \text{ mF} \quad M = 100 \text{ mH}$$

$$L_3 = 300 \text{ mH}$$

$$i_3 = i_1 + i_2$$

$$e_1 = \frac{1}{C_1} \int i_1 dt + L_1 \frac{di_1}{dt} - M \frac{di_3}{dt} + R_1 i_1 + R_3 i_3 + L_3 \frac{di_3}{dt} - M \frac{di_1}{dt}$$

$$e_2 = \frac{1}{C_2} \int i_2 dt + R_2 i_2 + R_3 i_3 + L_3 \frac{di_3}{dt} - M \frac{di_1}{dt}$$



$$\underline{E}_1 = 100 e^{j0} = 100$$

$$\underline{E}_2 = 100 e^{j\pi/2} = 100j$$

$$\underline{Z}_1 = j(\omega(L_1 - M) - \frac{1}{\omega C_1}) + R_1$$

$$= 2.5 + j(100 \cdot 10^{-1} - \frac{1}{100 \cdot 10^{-3}})$$

$$= 2.5$$

$$\left. \begin{aligned} \omega L &= \frac{1}{\omega C} \\ X_L &= X_C \end{aligned} \right\} \text{series resonance}$$

$$\underline{Z}_2 = j(\omega M - \frac{1}{\omega C_2}) + R_2 = 10 + j(100 \cdot 10^{-1} - \frac{1}{100 \cdot 10^{-3}}) = 10$$

$$\underline{Z}_3 = R_3 + j\omega(L_3 - M) = 10 + j100 \cdot 2 \cdot 10^{-1} = 10 + 20j = 10(1+2j)$$

$$\begin{cases} \underline{E}_1 = \underline{i}_1 \underline{Z}_1 + \underline{i}_3 \underline{Z}_3 \\ \underline{E}_2 = \underline{i}_3 \underline{Z}_3 + \underline{i}_2 \underline{Z}_2 \\ \underline{i}_3 = \underline{i}_1 + \underline{i}_2 \end{cases} \Leftrightarrow \begin{cases} 100 = 2.5 \cdot \underline{i}_1 + 10(1+2j)\underline{i}_3 & | : 2.5 \\ 100j = 10 \underline{i}_2 + 10(1+2j)\underline{i}_3 & | : 10 \\ \underline{i}_3 = \underline{i}_1 + \underline{i}_2 \Rightarrow \underline{i}_2 = \underline{i}_3 - \underline{i}_1 \end{cases}$$

$$\begin{cases} 40 = \underline{i}_1 + 4(1+2j)\underline{i}_3 \\ 10j = \underline{i}_3 - \underline{i}_1 + (1+2j)\underline{i}_3 \end{cases}$$

$$40 + 10j = (6+10j)\underline{i}_3 \Rightarrow \underline{i}_3 = \frac{(3+5j)(20-5j)}{425} = 425$$

$$\begin{aligned} \underline{i}_3 &= \frac{10(4+j)}{3+5j} = \frac{10(4+j)(3-5j)}{34} = \frac{5(4+j)(3-5j)}{34} = \frac{5}{2}(1-j) \\ &= \frac{5\sqrt{2}}{2} \left(\frac{\sqrt{2}}{2} - \frac{\sqrt{2}j}{2} \right) = \frac{5\sqrt{2}}{2} e^{j\frac{-\pi}{4}} \end{aligned}$$

$$i_3(t) = 5 \sin(100t + \frac{-\pi}{4})$$

$$40 = \underline{i}_1 + 4(1+2j) \cdot \frac{5}{2}(1-j)$$

$$40 = \underline{i}_1 + 10(3+j) \Rightarrow \underline{i}_1 = 10 - 10j = 10(1-j) = 10\sqrt{2} e^{j\frac{-\pi}{4}}$$

$$i_1(t) = 20 \sin(100t + (-\frac{\pi}{4}))$$

$$\underline{i}_2 = \underline{i}_3 - \underline{i}_1 \Rightarrow \underline{i}_2 = \frac{5}{2}(1-j) - 10(1-j) = -\frac{15}{2} + \frac{15}{2}j = -\frac{15}{2}(-1+j)$$

$$\underline{i}_2 = \frac{15\sqrt{2}}{2} e^{j\frac{3\pi}{4}}$$

$$i_2(t) = 15 \sin(100t + \frac{3\pi}{4})$$

$$\underline{V}_{C_1} = \underline{Z}_{C_1} \underline{i}_1 = \frac{-j}{100} \cdot 10(1-j) = \frac{-j}{100 \cdot 10^{-3}} 10(1-j) = -10j(10-10j)$$

$$= -100 - 100j = 100(-1-j) = 100\sqrt{2} e^{j\frac{5\pi}{4}}$$

$$\underline{V}_{C_2} = \underline{Z}_{C_2} \underline{i}_2 = \frac{-j}{10^{-1}} \cdot \underline{i}_2 = \frac{-j}{10^{-1}} \left(-\frac{15}{2} + \frac{15}{2}j\right) = -10j \left(-\frac{15}{2} + \frac{15}{2}j\right)$$

$$= 75j + 75 = 75(1+j) = 75\sqrt{2} \left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}j\right) = 75\sqrt{2} e^{j\pi/4}$$

$$\underline{S}_{\text{gen}} = \underline{S}_{\text{rec}}$$

$$\underline{S}_{\text{rec}} = \underline{Z}_1 \underline{i}_1^2 + \underline{Z}_2 \underline{i}_2^2 + \underline{Z}_3 \underline{i}_3^2 = 2.5 \cdot 200 + 10 \cdot \frac{225}{2} + 10(1+2j) \cdot \frac{25}{3}$$

$$= 500 + 1125 + 125 + 250j = 250(7+j)$$

$$\underline{S}_{\text{gen}} = \underline{E}_1 \cdot \underline{i}_1^* + \underline{E}_2 \cdot \underline{i}_2^* = 100 \cdot 10(1+j) + 100j \cdot \frac{15}{2} (-1-j)$$

$$= 1000 + 100j - 750j + 750 = 250(7+j)$$

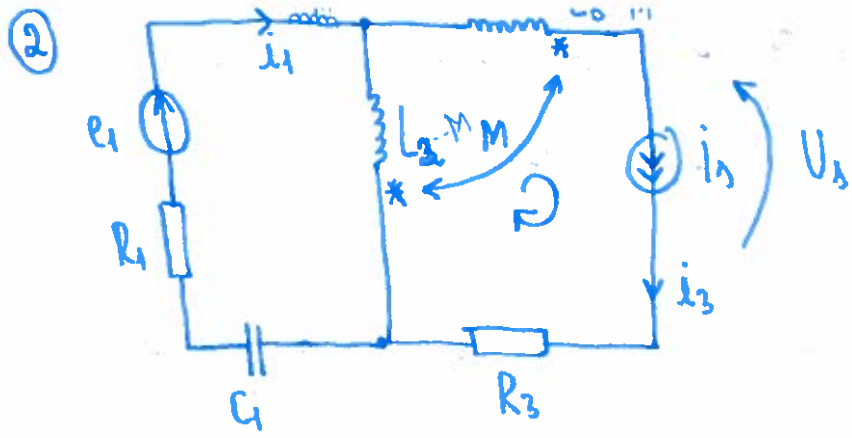
Node Potential Method

$$V_2 = 0$$

$$Y_{11} V_1 = I_{\text{sc}1}$$

$$Y_{11} = \frac{1}{\underline{Z}_1} + \frac{1}{\underline{Z}_2} + \frac{1}{\underline{Z}_3}$$

$$I_{\text{sc}1} = \frac{E_1}{\underline{Z}_1} + \frac{E_2}{\underline{Z}_2}$$



$$R_1 = 2 \Omega \quad C_1 = \frac{10}{\pi} \text{ mF}$$

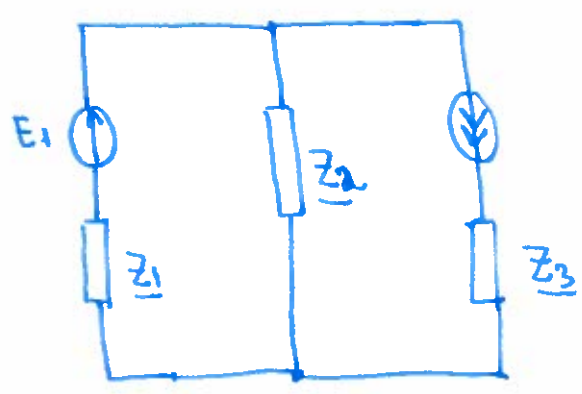
$$\omega = 50 \text{ Hz}$$

$$L_2 = \frac{30}{\pi} \text{ mH} \quad L_3 = M = \frac{10}{\pi} \text{ mH}$$

$$e_1(t) = 16 \sin\left(\omega t + \frac{\pi}{4}\right)$$

$$i_3(t) = 4\sqrt{2} \cos \omega t$$

$$\begin{cases} i_1 = i_2 + i_3 \\ e_1 = R_1 i_1 + \frac{1}{C_1} \int i_1 dt + L_2 \frac{di_2}{dt} + M \frac{di_3}{dt} \\ 0 = R_3 i_3 + L_3 \frac{di_3}{dt} + M \frac{di_2}{dt} - U_3 - L_2 \frac{di_2}{dt} - M \frac{di_3}{dt} \end{cases}$$



$$\underline{Z}_1 = 2$$

$$\underline{E}_1 = 8\sqrt{2} e^{j\frac{\pi}{4}} = 8\sqrt{2} \left(\frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2}j\right) = 8(1+j)$$

$$\underline{i}_3 = 4 e^{j\frac{\pi}{2}} = 4j$$

$$\underline{Z}_1 = \underline{R}_1 + j\left(-\frac{1}{\omega C_1} + \omega M\right)$$

$$= 2 + j\left(\frac{-1}{2 \cdot 50 \pi \cdot \frac{10}{\pi} \cdot 10^{-3}} + 2 \cdot 50 \cdot \pi \cdot \frac{10}{\pi} \cdot 10^{-3}\right)$$

$$\underline{Z}_2 = j\omega(L_2 - M) = j \cdot 2 \cdot 50 \cdot \pi \cdot \frac{20}{\pi} \cdot 10^{-3} = 2j$$

$$\underline{Z}_3 = j\omega(L_3 - M) = 1$$

$$\begin{cases} \underline{Z}_{11} \underline{i}_1' + \underline{Z}_{12} \underline{i}_2' = \underline{E}_1' \\ \underline{i}_2' = \underline{i}_3 = 4j \end{cases}$$

$$2(1+j) \underline{i}_2' - 2j \cdot 4j = 8(1+j)$$

$$2(1+j) \underline{i}_1' = 8j \Rightarrow \underline{i}_1' = \frac{8j}{2(1+j)} \Rightarrow \underline{i}_1' = 2(1+j)$$

$$\underline{i}_1 = \underline{i}_1'$$

$$\underline{i}_2 = \underline{i}_1' - \underline{i}_2'$$

$$\underline{U}_s + \underline{Z}_2 \underline{i}_2 - \underline{Z}_3 \underline{i}_3 = 0$$

$$\underline{S}_{\text{gen}} = \underline{E}_1 \underline{i}_1^* + \underline{U}_s \underline{i}_s^*$$